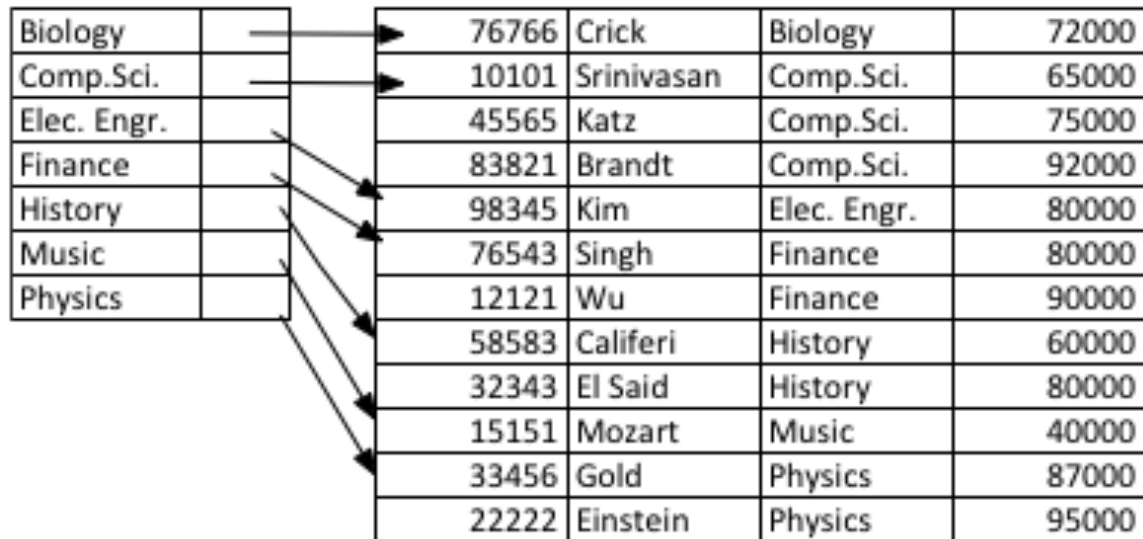


# Dense Index

10101	→	10101	Srinivasan	Comp.Sci.	65000
12121	→	12121	Wu	Finance	90000
15151	→	15151	Mozart	Music	40000
22222	→	22222	Einstein	Physics	95000
32343	→	32343	El Said	History	80000
33456	→	33456	Gold	Physics	87000
45565	→	45565	Katz	Comp.Sci.	75000
58583	→	58583	Califeri	History	60000
76543	→	76543	Singh	Finance	80000
76766	→	76766	Crick	Biology	72000
83821	→	83821	Brandt	Comp.Sci.	92000
98345	→	98345	Kim	Elec. Engr.	80000

From Silberschatz, et.al., *Database Systems Concepts*, 6<sup>th</sup> ed

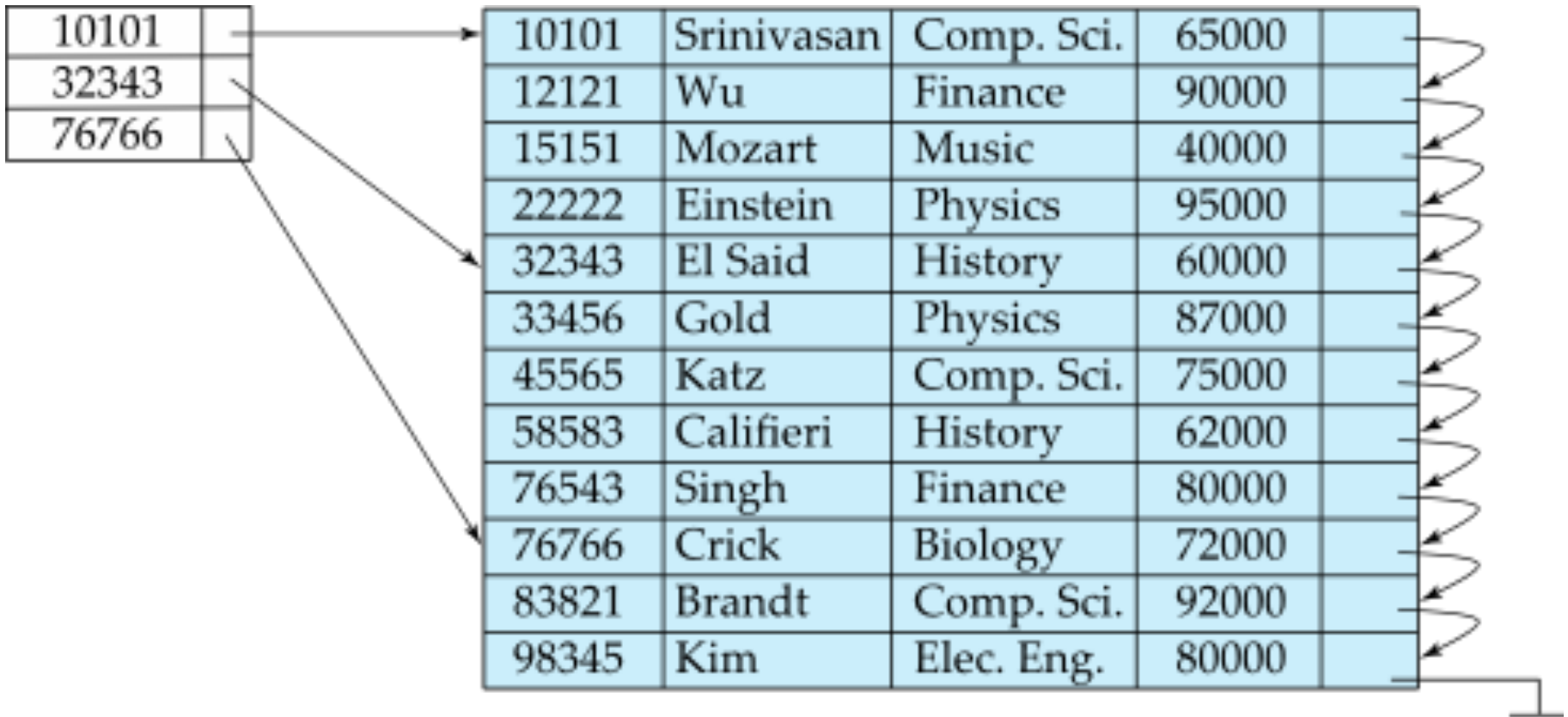
## Dense Index sorted on other than primary key



Biology	→	76766	Crick	Biology	72000
Comp.Sci.	→	10101	Srinivasan	Comp.Sci.	65000
Elec. Engr.	→	45565	Katz	Comp.Sci.	75000
Finance	→	83821	Brandt	Comp.Sci.	92000
History	→	98345	Kim	Elec. Engr.	80000
Music	→	76543	Singh	Finance	80000
Physics	→	12121	Wu	Finance	90000
		58583	Califeri	History	60000
		32343	El Said	History	80000
		15151	Mozart	Music	40000
		33456	Gold	Physics	87000
		22222	Einstein	Physics	95000

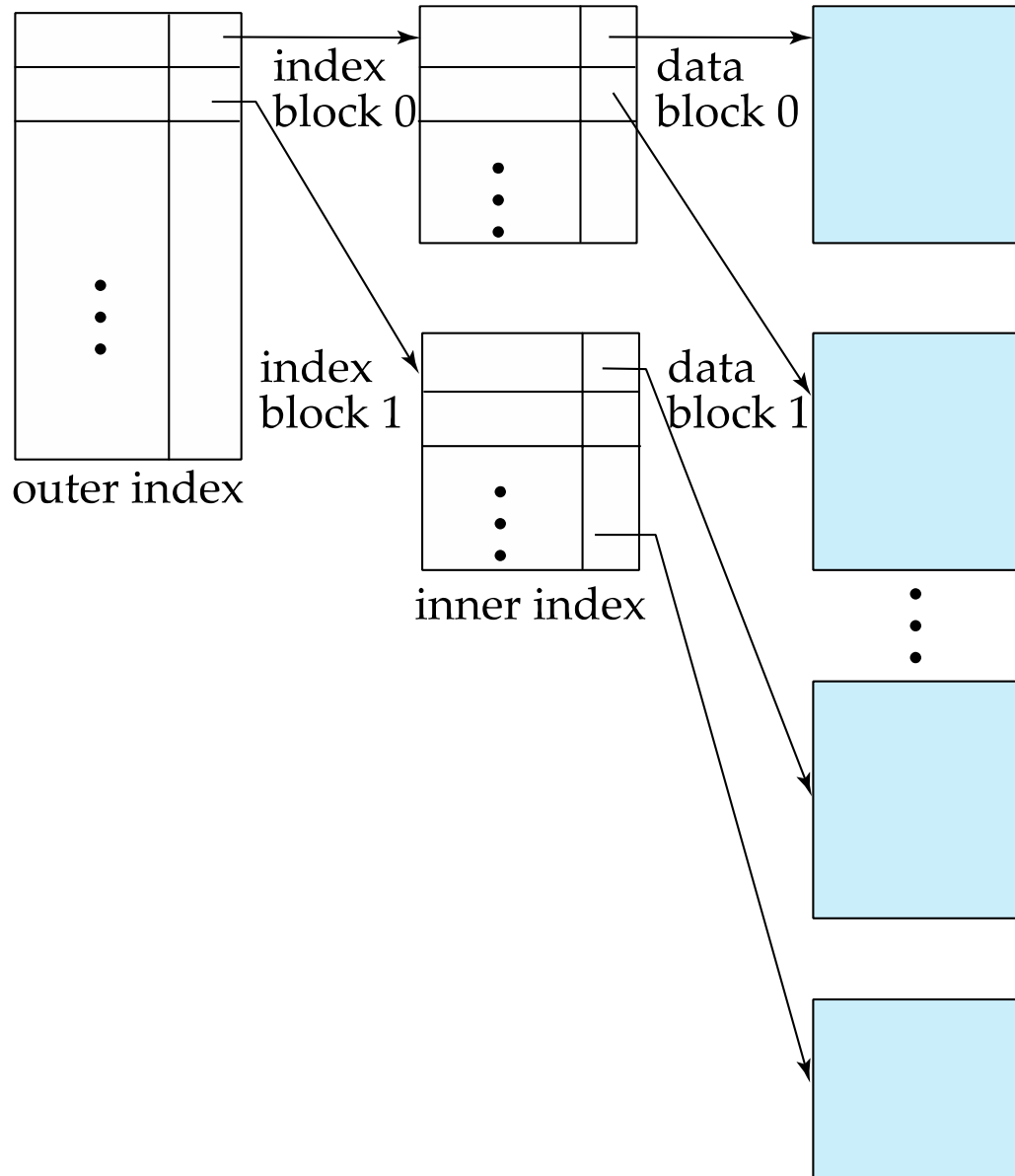
From Silberschatz, et.al., *Database Systems Concepts*, 6<sup>th</sup> ed.

# Sparse index

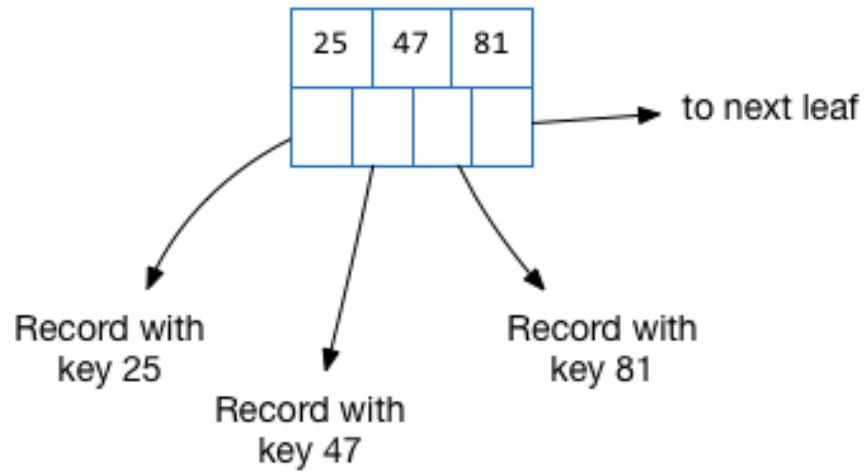


From Silberschatz, et.al., *Database Systems Concepts*, 6<sup>th</sup> ed.

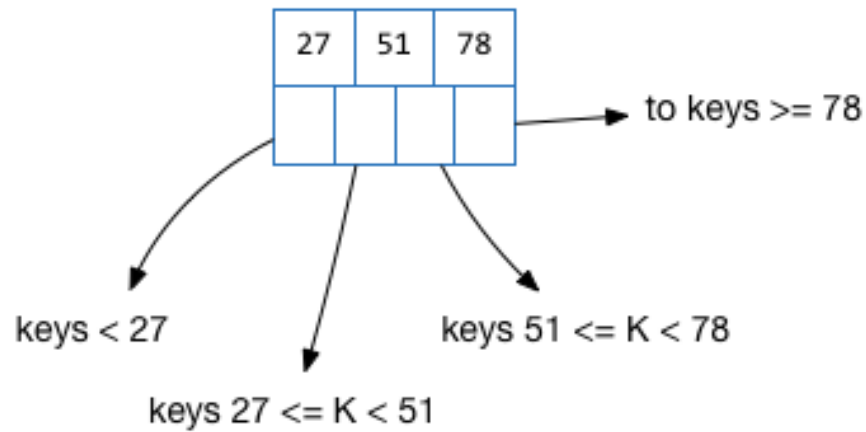
# Multi-Level Index



## Leaf of a B+ Tree



## Interior node of a B+ Tree



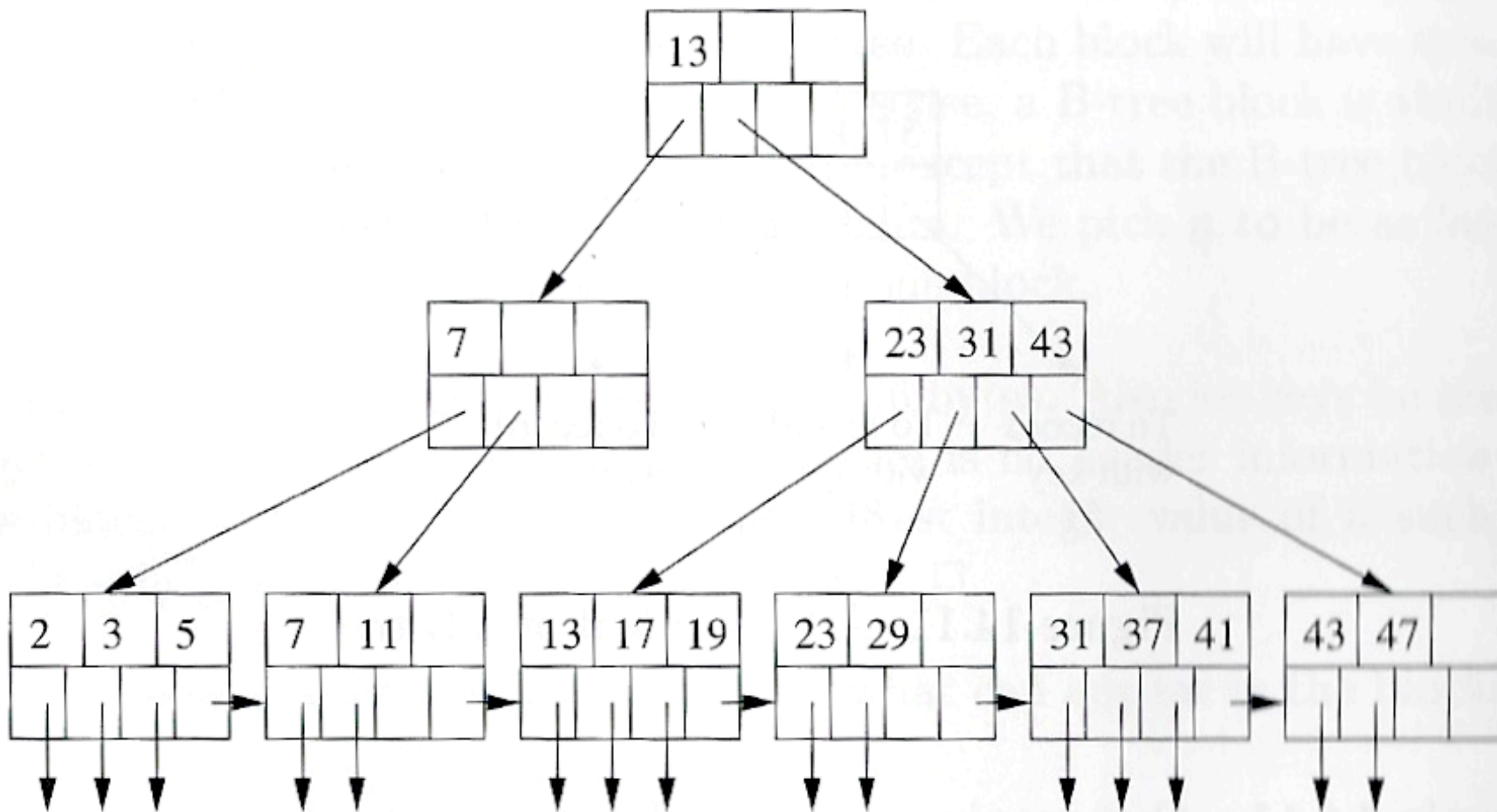


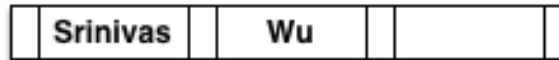
Figure 14.13: A B-tree

## Example of B+-Tree - building from the instructor table

Step 1. Insert Srinivas



Step 2. Insert Wu



Step 3. Insert Mozart

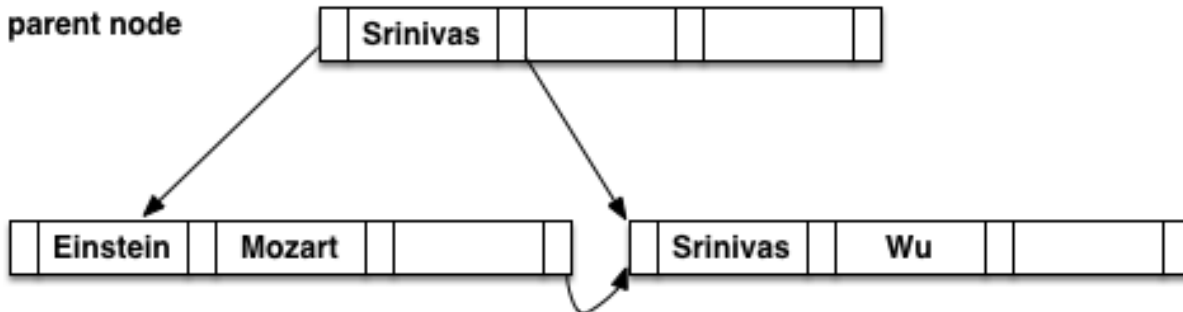


Step 4. Insert Einstein

Step 4a. Split the root node

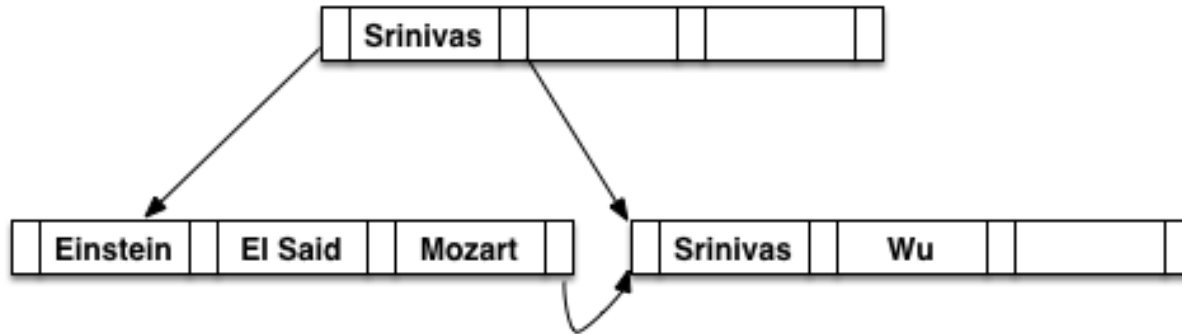


Step 4b. Create a new parent node





**Step 5. Insert El Said**

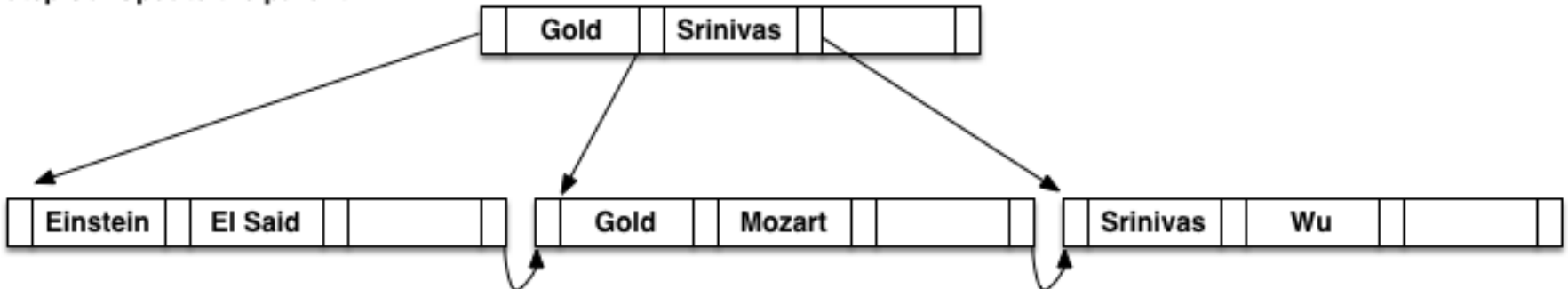


**Step 6. Insert Gold**

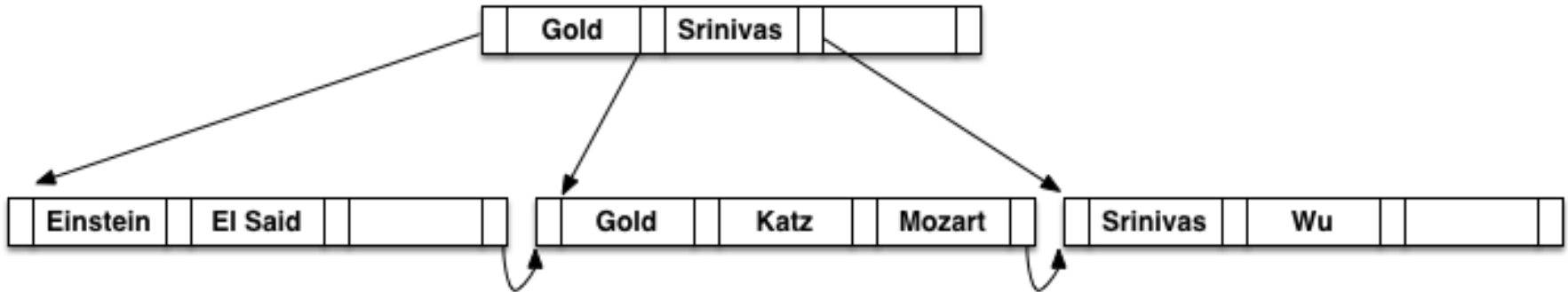
**Step 6a: Overflowed the node, so split it**



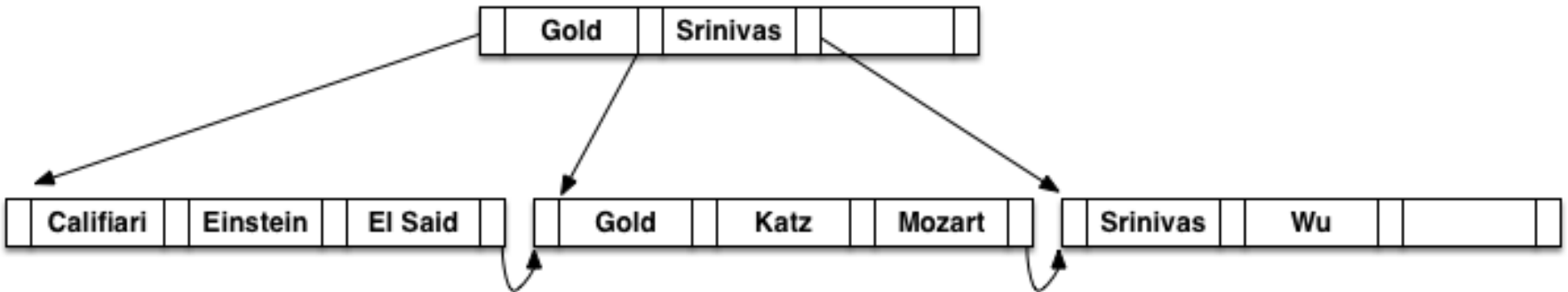
**Step 6b: Update the parent**



Step 7. Insert Katz



Step 8. Insert Califari

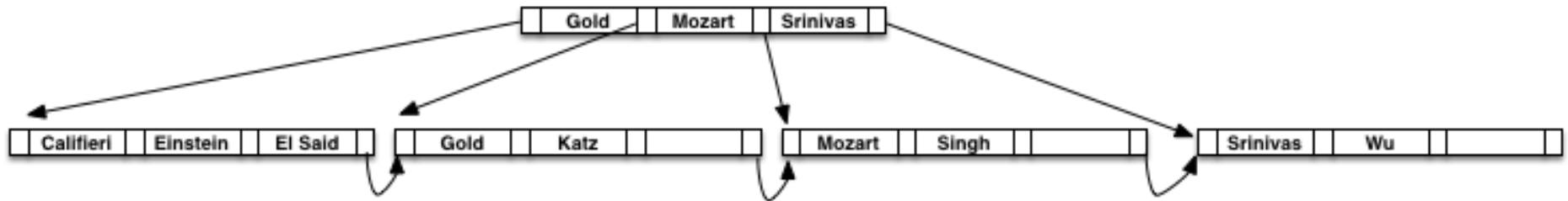


### Step 9: Insert Singh

Step 9a: overflowed the node, so split it

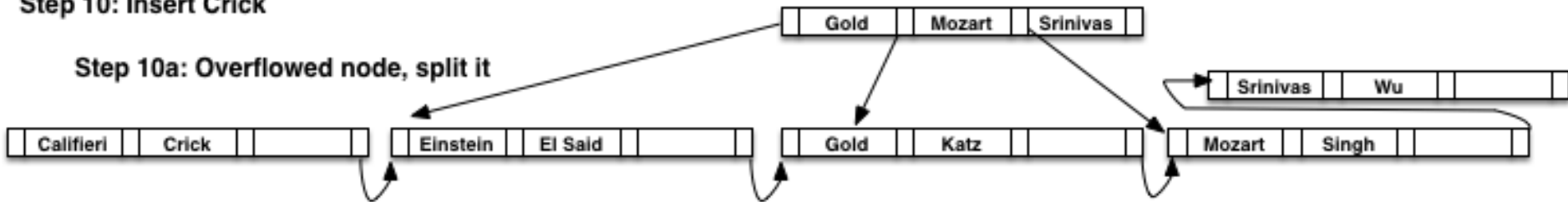


Step 9b: update parent

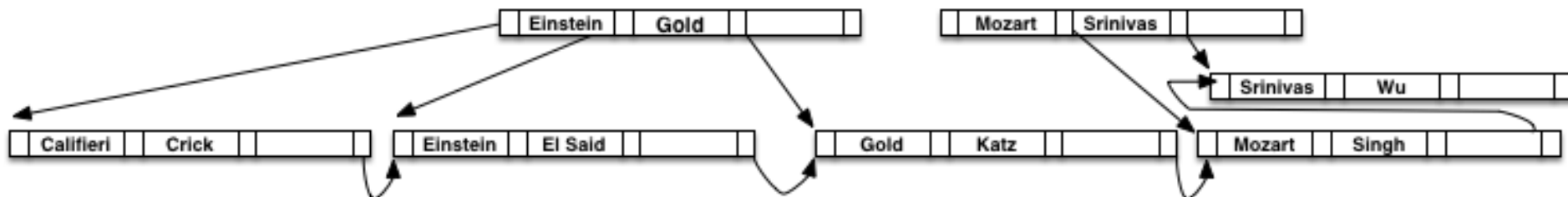


### Step 10: Insert Crick

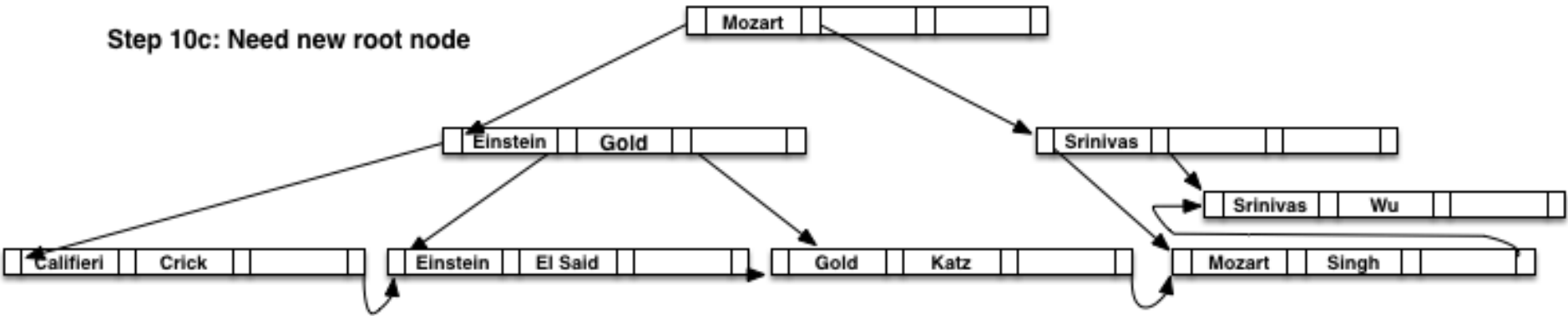
Step 10a: Overflowed node, split it



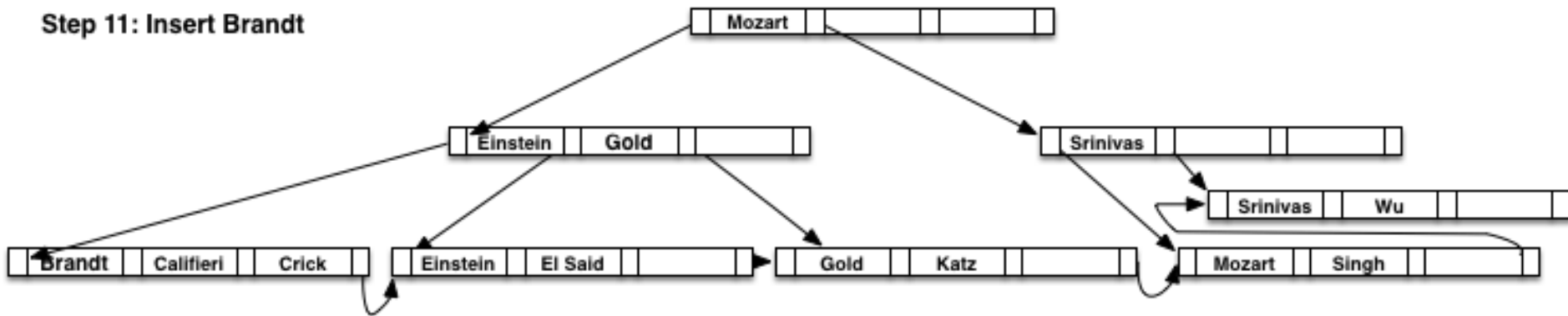
Step 10b: Update parent, but overflowed parent node, split it



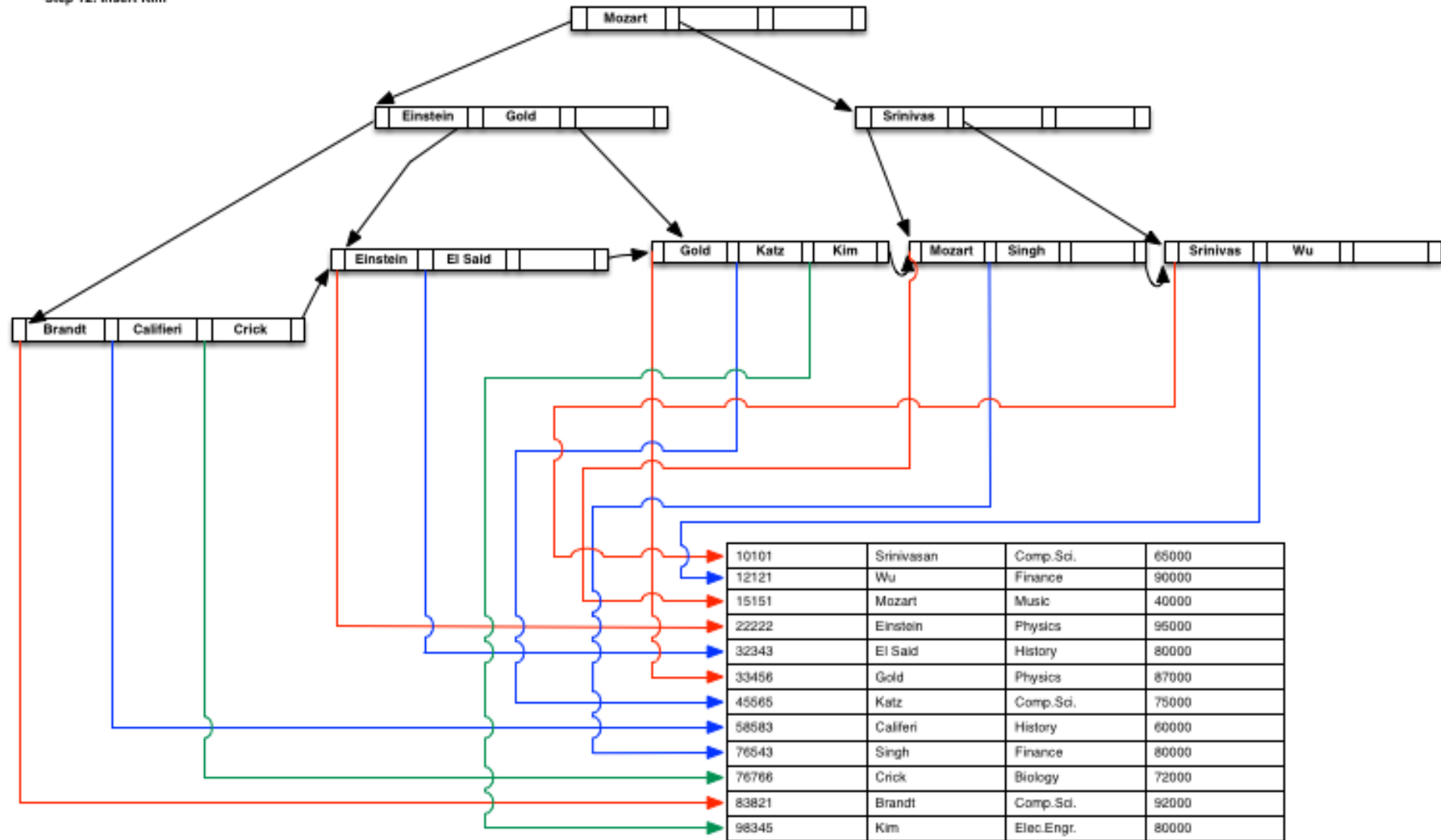
Step 10c: Need new root node



Step 11: Insert Brandt



Step 12: Insert Kim



From Silberschatz, et.al., *Database Systems Concepts*, 6<sup>th</sup> ed., updated by CCPalmer

## Players

ID	Name	Club	Salary
66145	Alice	MWU	80000
35643	Boris	FCB	89000
49511	Carlos	MC	76000
62944	Dean	UF	78000
68288	Eve	MWU	93500
91026	Fabio	FCB	95000
14838	Gina	LFC	82000
53062	Hector	FCB	92000
74400	Ignatio	LFC	67700
76190	Jose	GFC	81800
84231	Kyle	GFC	77700
56190	Luis	CFC	82000

## Hash Values

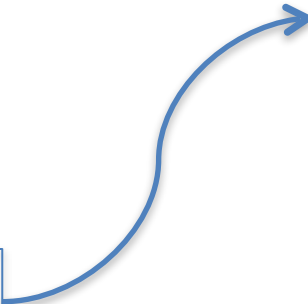
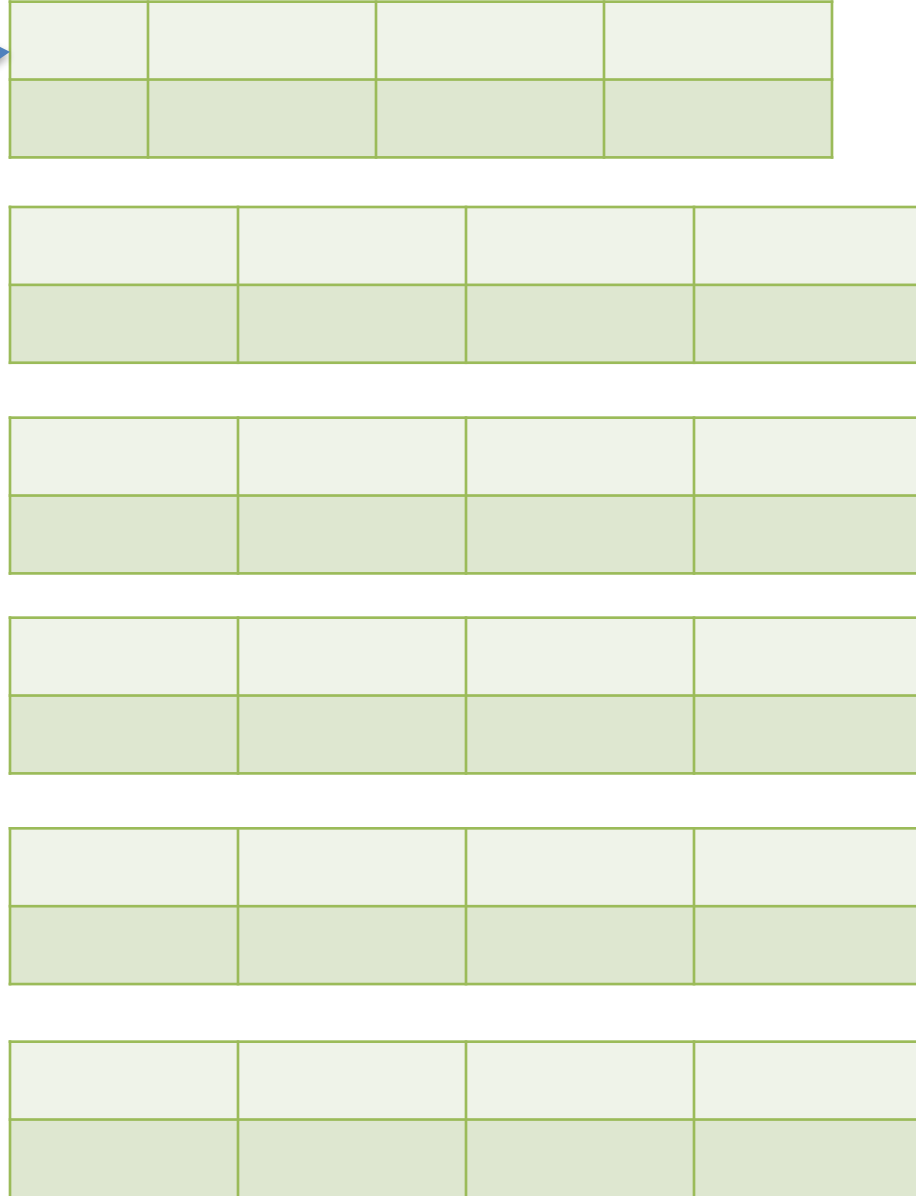
Club	hash(Club)		
CFC	00111111	10101100	00010000
FCB	11111001	10010000	00100111
GFC	11000111	10010001	01111100
LFC	10010110	00000111	00100100
MC	01001101	11101110	00000101
MWU	10100010	11000010	01011111
UF	00110011	01110010	00001110

Hash prefix

0

Index players by club hash

0



Bucket Pointer Table

Hash prefix

1

1. Insert Dean, Fabio, & Alice.

0
1

Bucket Pointer Table

62944	Dean	UF	78000	1
				001
91026	Fabio	FCB	95000	1
66145	Alice	MWU	80000	111
				101



## 2. Insert Gina, causing a split

Hash prefix

2

00
01
10
11

Bucket Pointer Table

62944	Dean	UF	78000	1	001
14838	Gina	LFC	72000	2	100
66145	Alice	MWU	80000		101
91026	Fabio	FCB	95000	2	111

### 3. Insert Ignatio & Kyle

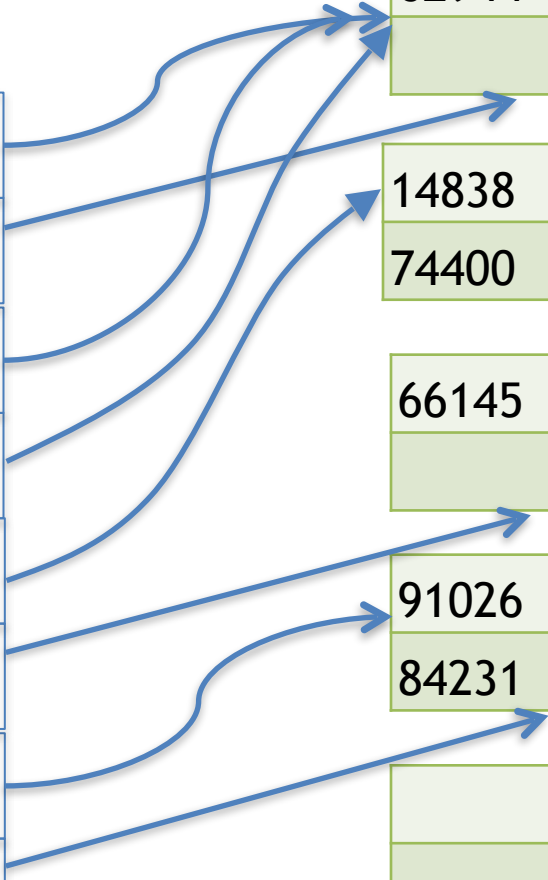
Hash prefix

3

000
001
010
011
100
101
110
111

Bucket Pointer Table

62944	Dean	UF	78000	1	001
14838	Gina	LFC	72000	3	100
74400	Ignatio	LFC	67700		100
66145	Alice	MWU	80000	3	101
91026	Fabio	FCB	95000	2	111
84231	Kyle	GFC	77700		110



#### 4. Insert Boris

Hash prefix

3

000
001
010
011
100
101
110
111

62944	Dean	UF	78000	1	001

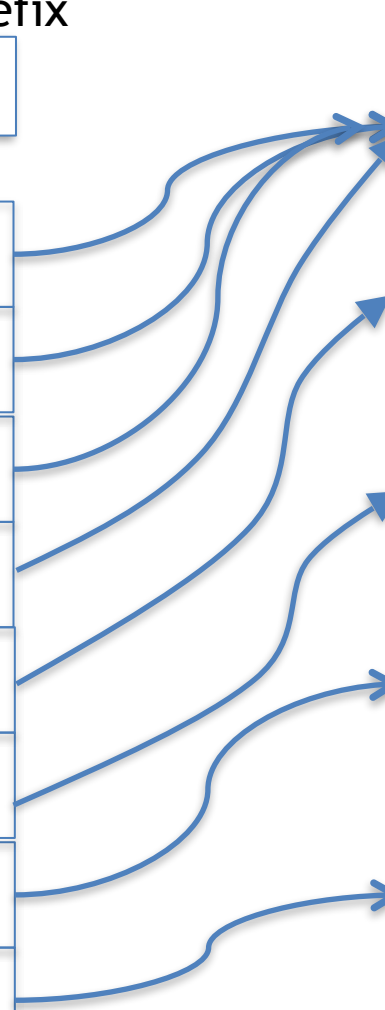
14838	Gina	LFC	72000	3	100
74400	Ignatio	LFC	67700		100

66145	Alice	MWU	80000	3	101

84231	Kyle	GFC	77700	3	110

91026	Fabio	FCB	95000	3	111
35643	Boris	FCB	89000		111


Bucket Pointer Table



## 5. Insert Luis, Hector, Jose, & Eve

Hash prefix

3

000
001
010
011
100
101
110
111

Bucket Pointer Table

62944	Dean	UF	78000	2	001
56190	Luis	CFC	82000		001
14838	Gina	LFC	72000	3	100
74400	Ignatio	LFC	67700		100
66145	Alice	MWU	80000	3	101
68288	Eve	MWU	83500		101
84231	Kyle	GFC	77700	3	110
76190	Jose	GFC	81800		110
91026	Fabio	FCB	95000	3	111
35643	Boris	FCB	89000		111
53062	Hector	FCB	92000		111

## 6. Insert Carlos.

Hash prefix

3

000
001
010
011
100
101
110
111

Bucket Pointer Table

62944	Dean	UF	78000	2	001
56190	Luis	CFC	82000		001
49511	Carlos	MC	76000	2	010
14838	Gina	LFC	72000	3	100
74400	Ignatio	LFC	67700		100
66145	Alice	MWU	80000	3	101
68288	Eve	MWU	83500		101
84231	Kyle	GFC	77700	3	110
76190	Jose	GFC	81800		110
91026	Fabio	FCB	95000	3	111
35643	Boris	FCB	89000		111
53062	Hector	FCB	92000		111

*Now sorted by team hash!*

# Bitmap Indices

record number	ID	gender	income_level
0	76766	m	L1
1	22222	f	L2
2	12121	f	L1
3	15151	m	L4
4	58583	f	L3

Bitmaps for *gender*

m 10010

f 01101

Bitmaps for *income\_level*

L1 10100

L2 01000

L3 00001

L4 00010

L5 00000

```
SELECT *
FROM Table
WHERE gender='f' AND income_level = 'L2'
```

⇒ 01101  $\wedge$  01000 = 01000

# Bitmap Indices

Record #	ID	Grad	Income Level
0	76766	Yes	L1
1	22223	No	L2
2	12641	No	L1
3	86538	Yes	L4
4	49650	No	L3

Bitmaps for  
*College grad*

Yes 10010  
No 01101

Bitmaps for  
*Income Level*

10100  
01000  
00001  
00010  
00000

⇒  $01101 \wedge 01000 = 01000$

```
SELECT *
FROM Table
WHERE Grad="No" AND income_level = 'L2'
```